

The cosmic emergence* of thin discs

Order out of Chaos:
secular thick and thin disc settling

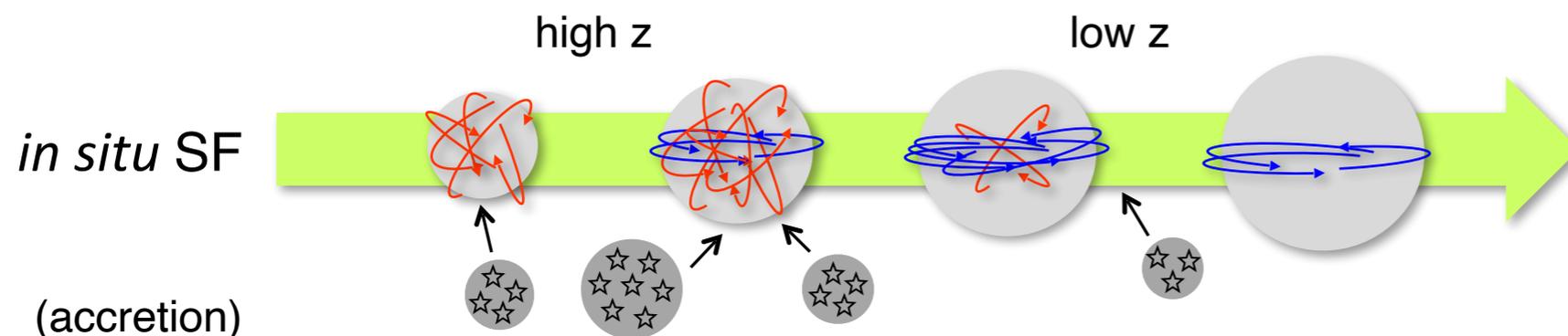
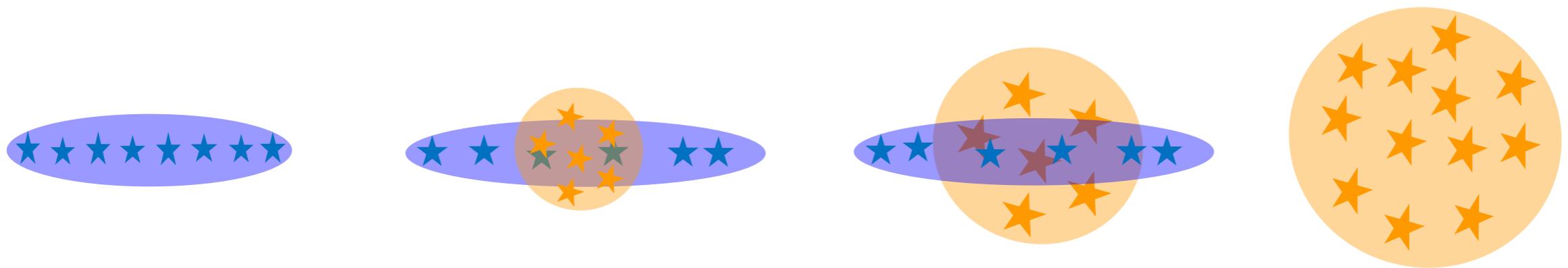
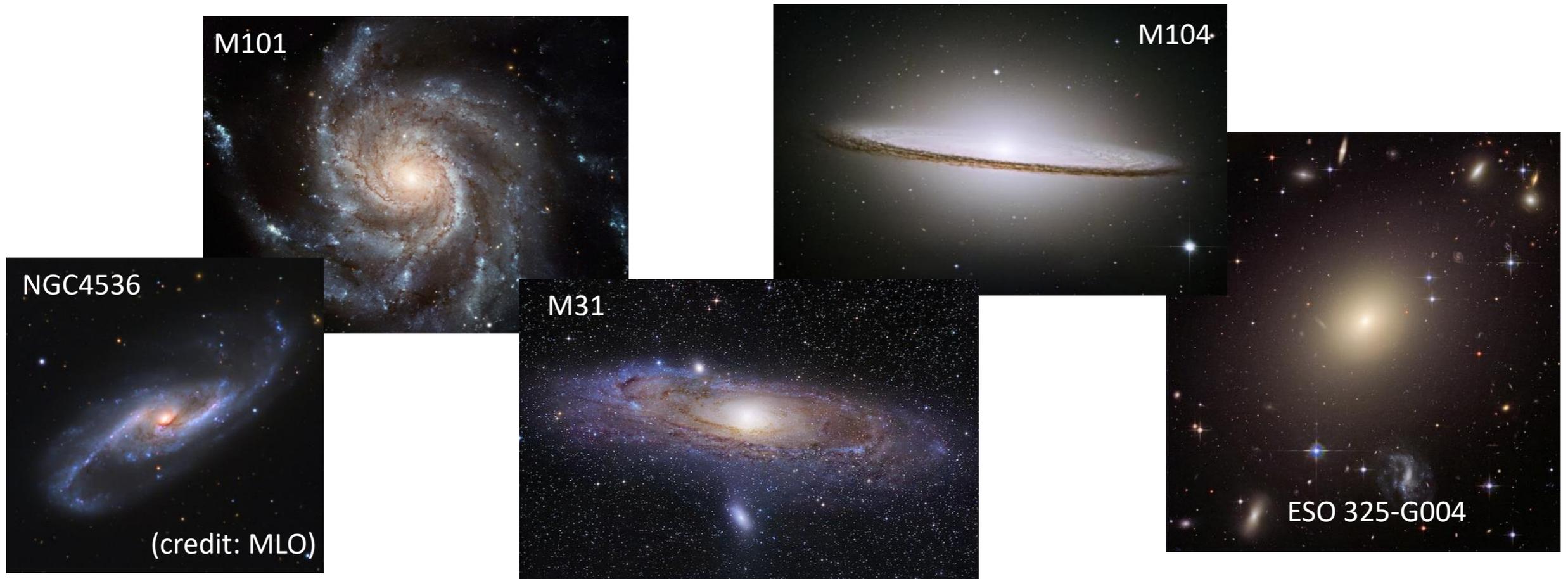
* **emergence** = the arising of novel and coherent structures through self-organization in complex systems

Christophe Pichon & The NewHorizon Collaboration (Min-Jung Park++)

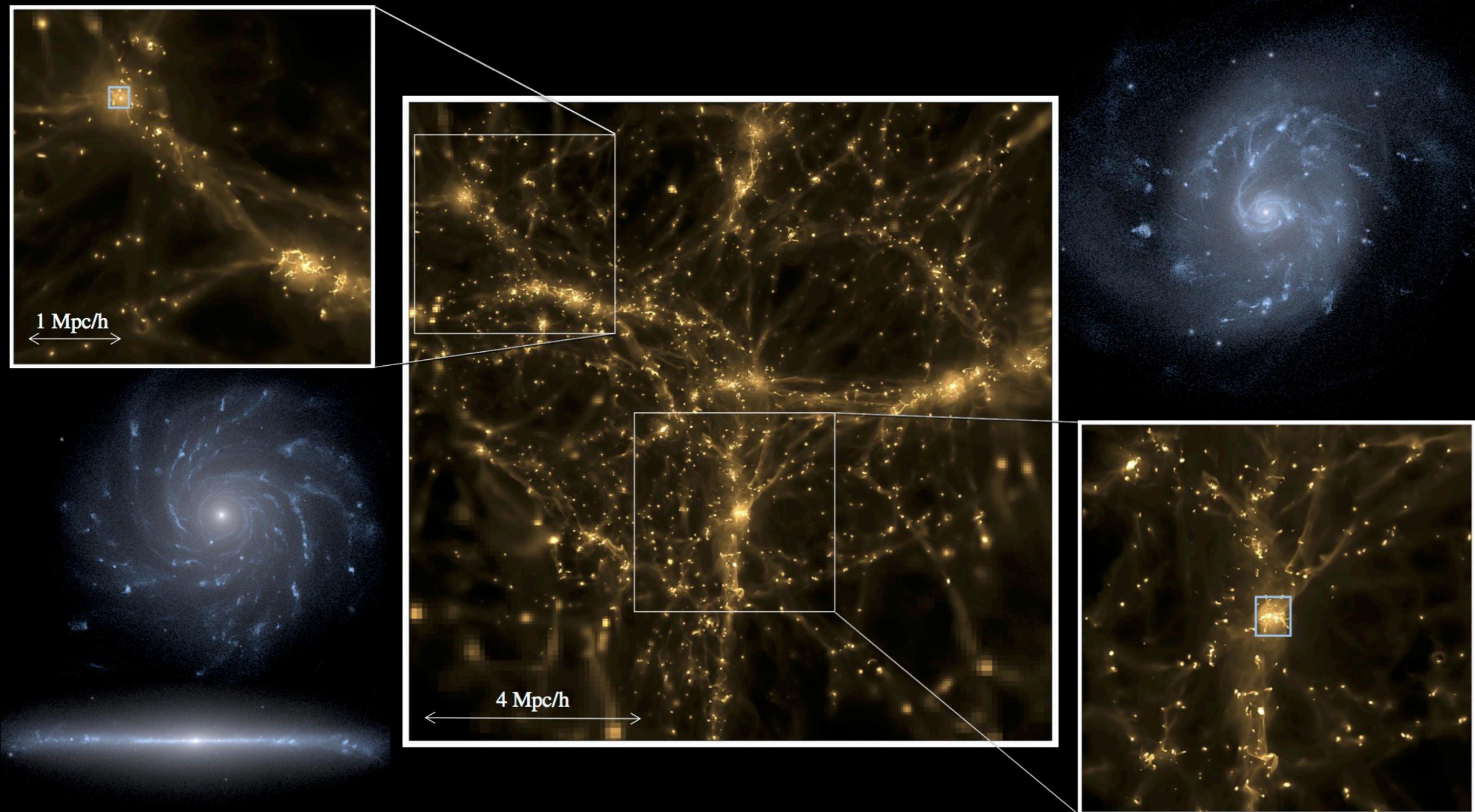
Understanding formation of massive thin discs?

Diverse morphologies of galaxies

(Credit: NASA, ESA and STScI)



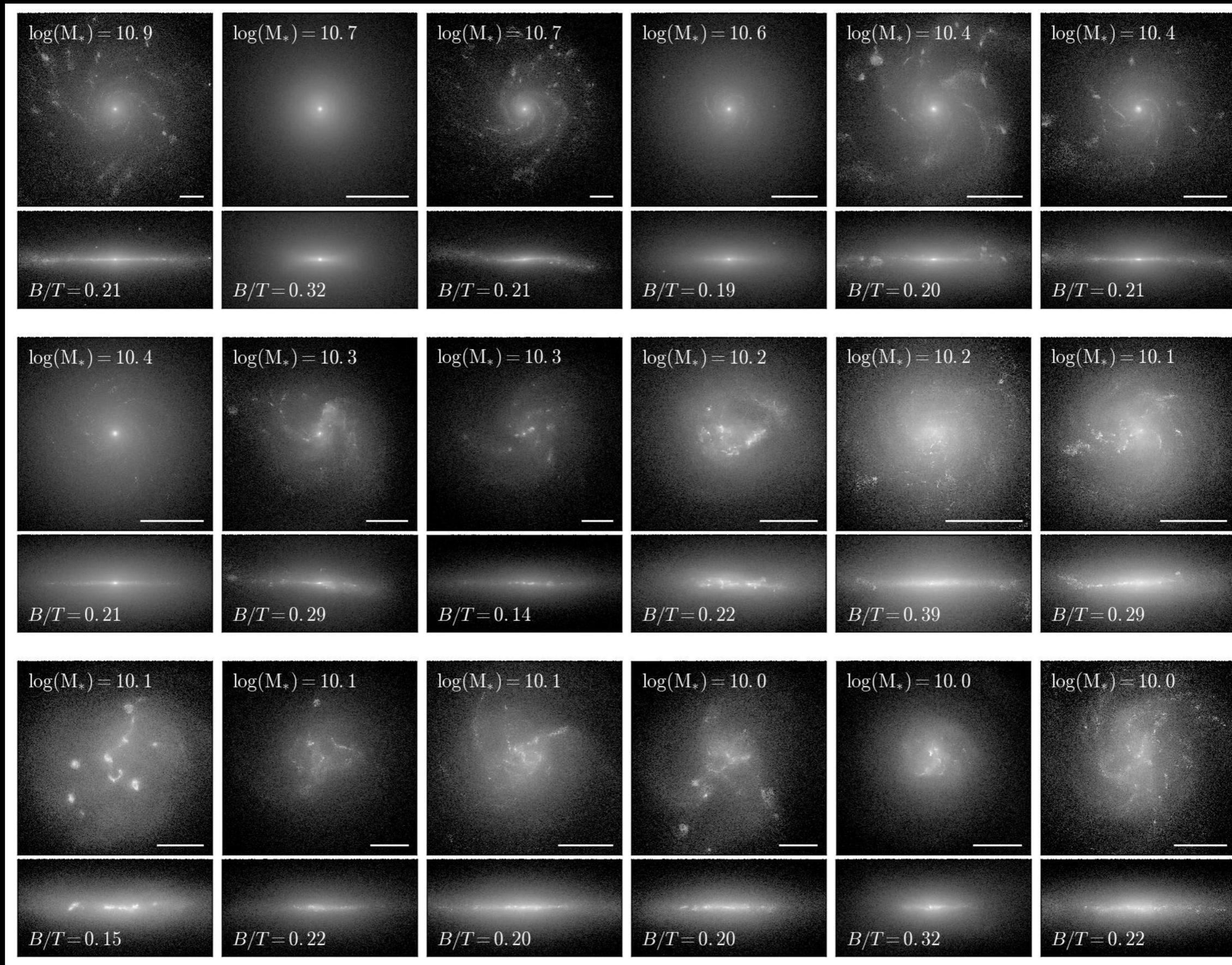
The New Horizon simulation



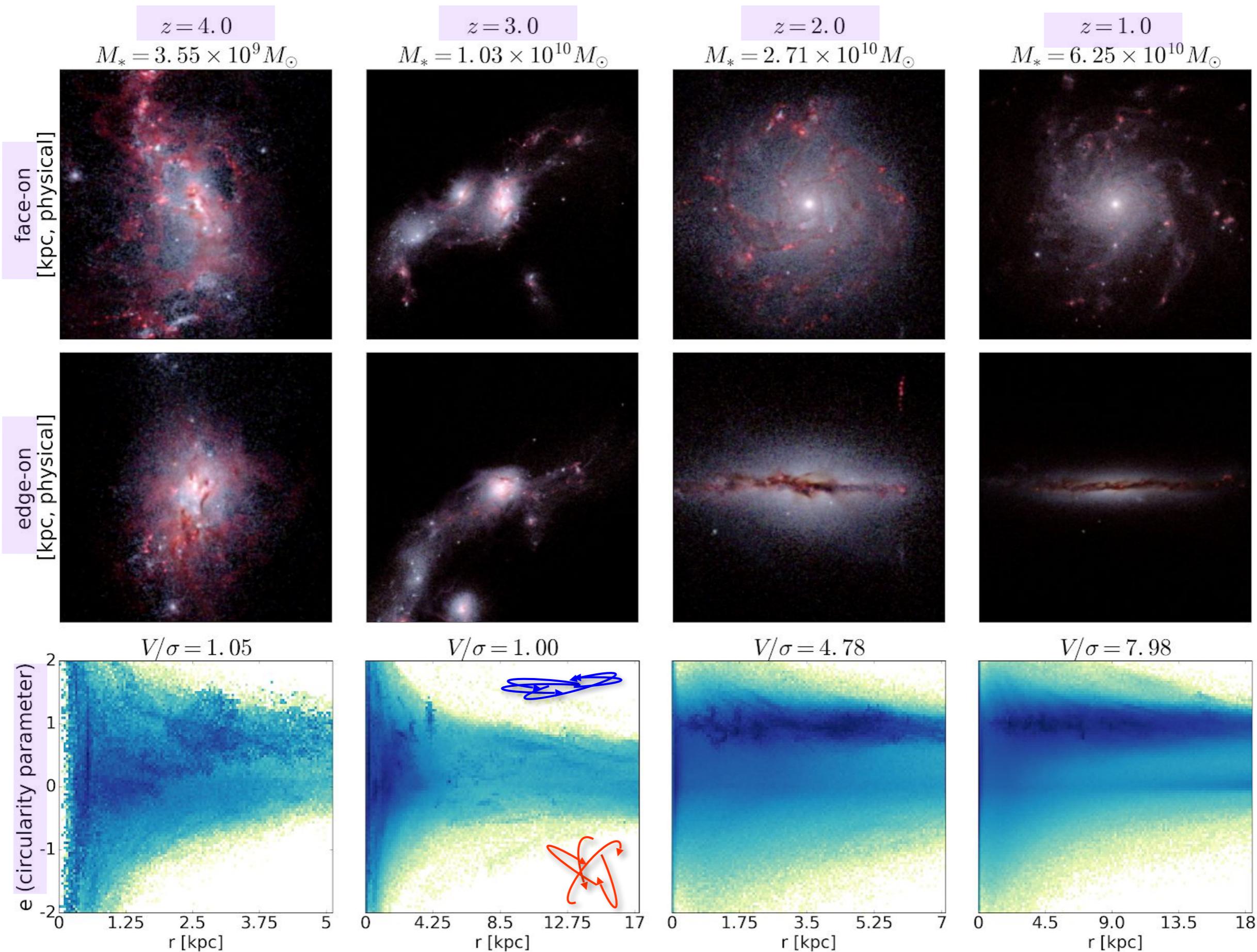
New Horizon Simulation

(c) M Park 2020

Other examples (out of 1000s)

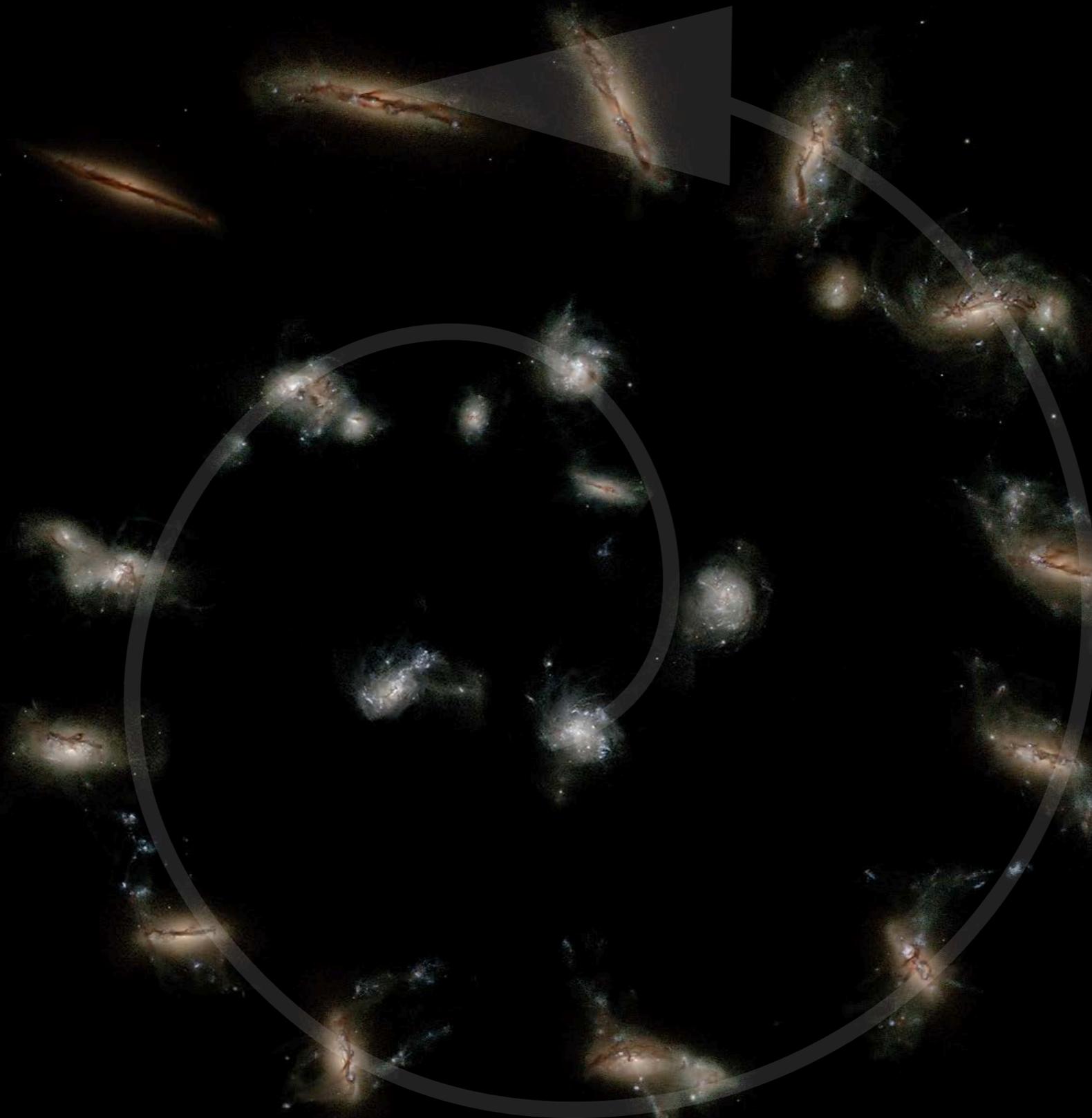


Disc settling: numerical evidence



Disc settling: timeline of a thin galactic disc

New Horizon Simulation



- Environment need to detune & stellar component to dominate: secular mode

- Why do disc settle ? Because $Q \rightarrow 1$
- But Why does $Q \rightarrow 1$? Because tighter control loop ($t_{\text{dyn}} \ll 1$) via **wake**
- But how does it impact settling? Because wake also **stiffens** coupling

New Horizon

Ring toy model

- Convergence towards $Q \sim 1$
 - is dual to settled fraction of discs increasing with mass and cosmic time
 - implies that thick and thin discs grow together

Synopsis of presentation

7

- Environment need to detune & stellar component to dominate: secular mode

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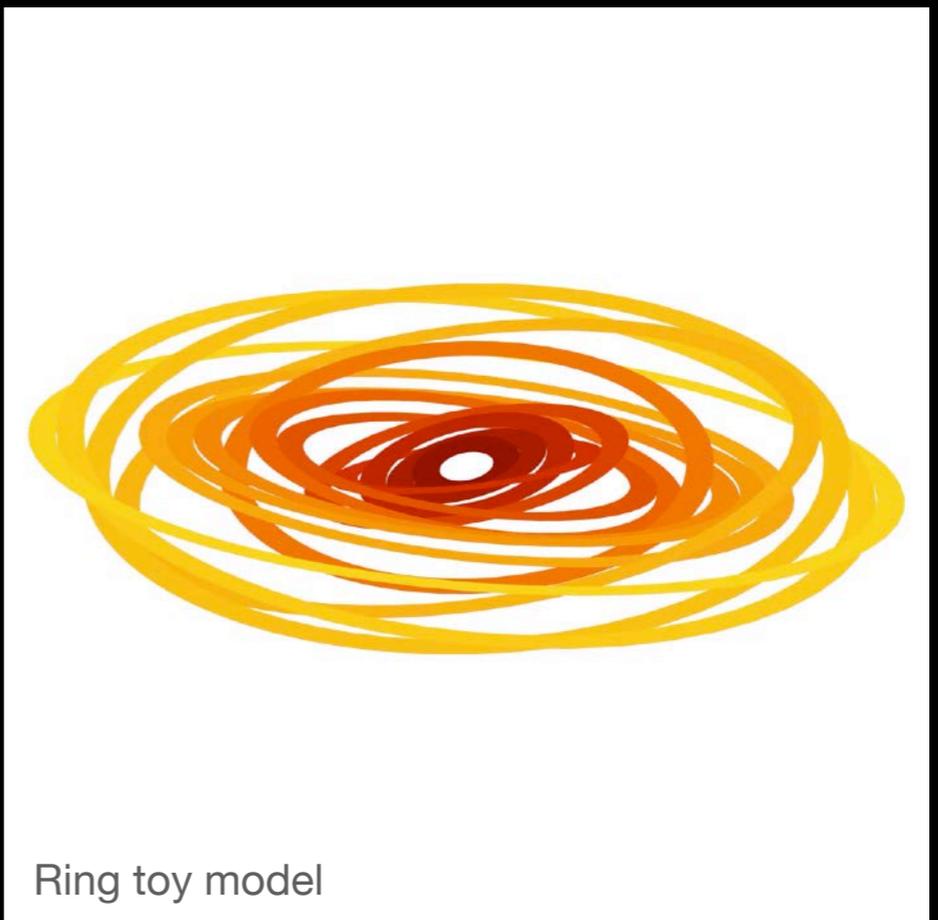
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New Horizon

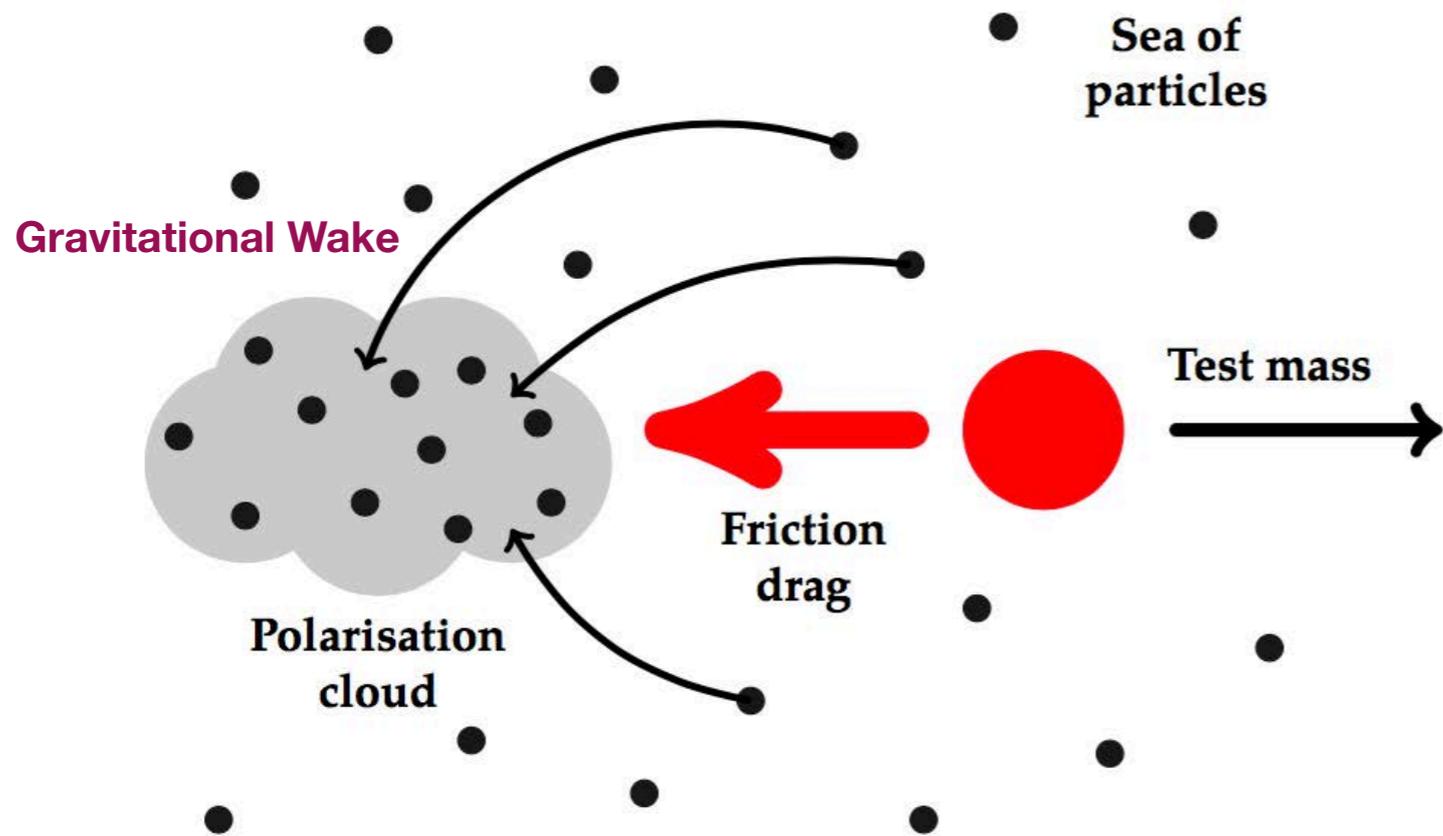


Ring toy model

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Gravitational wake/polarisation/dressing

Chandrasekhar polarisation

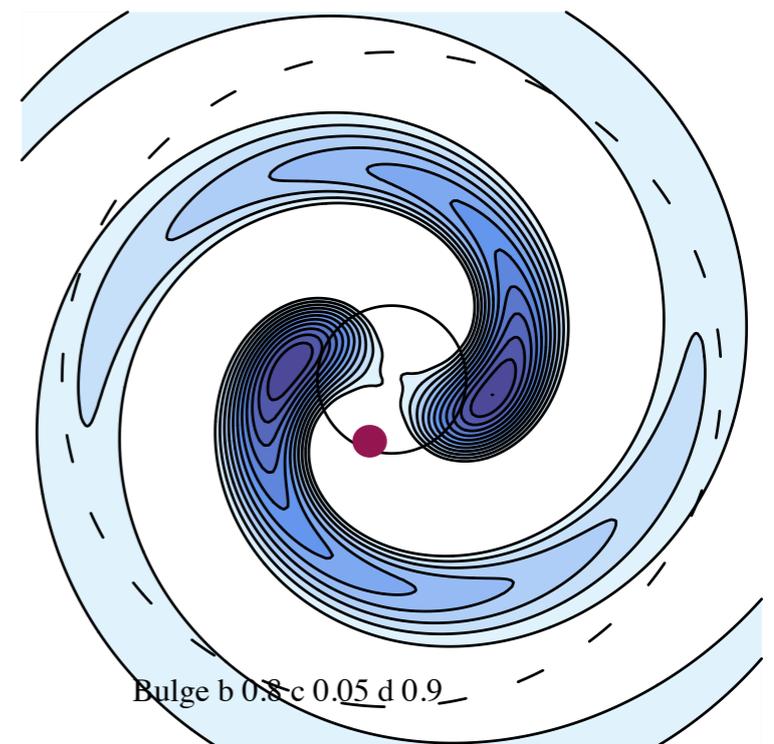
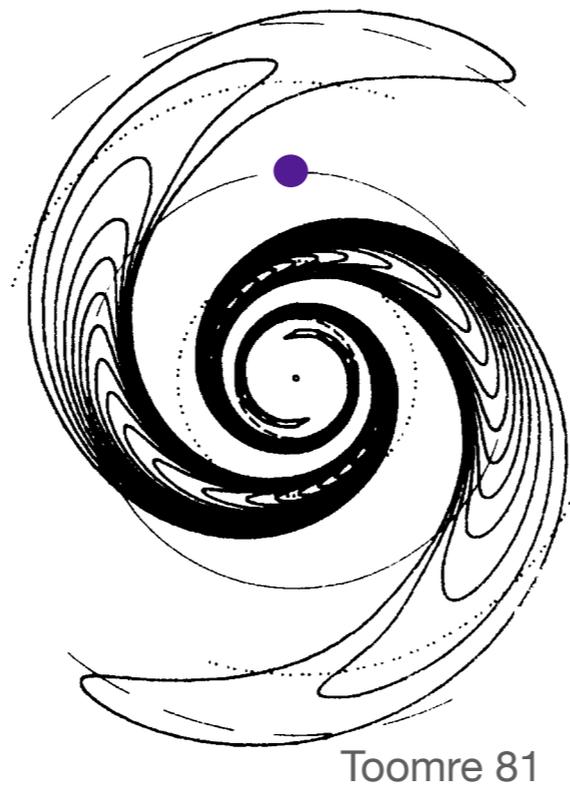
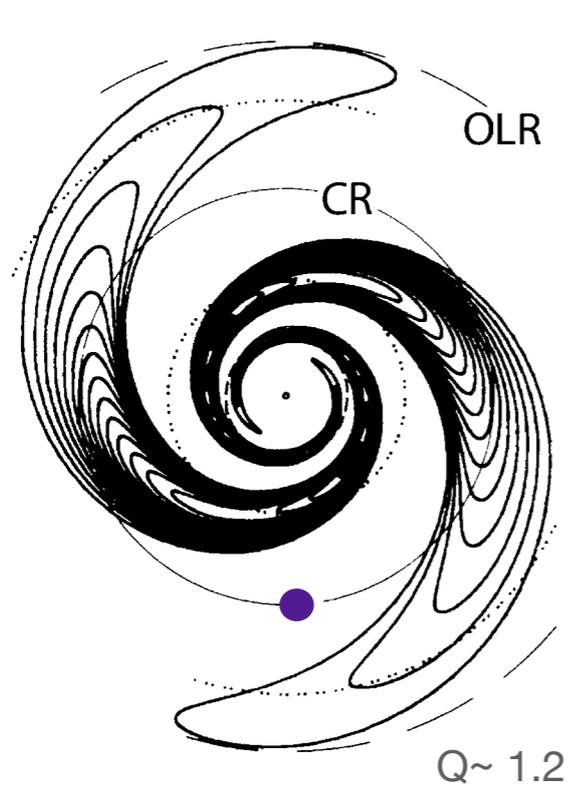


$$[\delta\psi]_{\text{dressed}} = \frac{[\delta\psi]_{\text{bare}}}{|\epsilon(\omega)|}$$

$$T_{\text{dressed}} \approx |\epsilon| T_{\text{bare}}$$

$$\Omega_{\text{dressed}} \approx \frac{1}{|\epsilon|} \Omega_{\text{bare}}$$

Mass in **wake** = mass of perturbation **X 140 !!** $\neq 1.8$ for sphere



On the importance of *gravitational wakes*

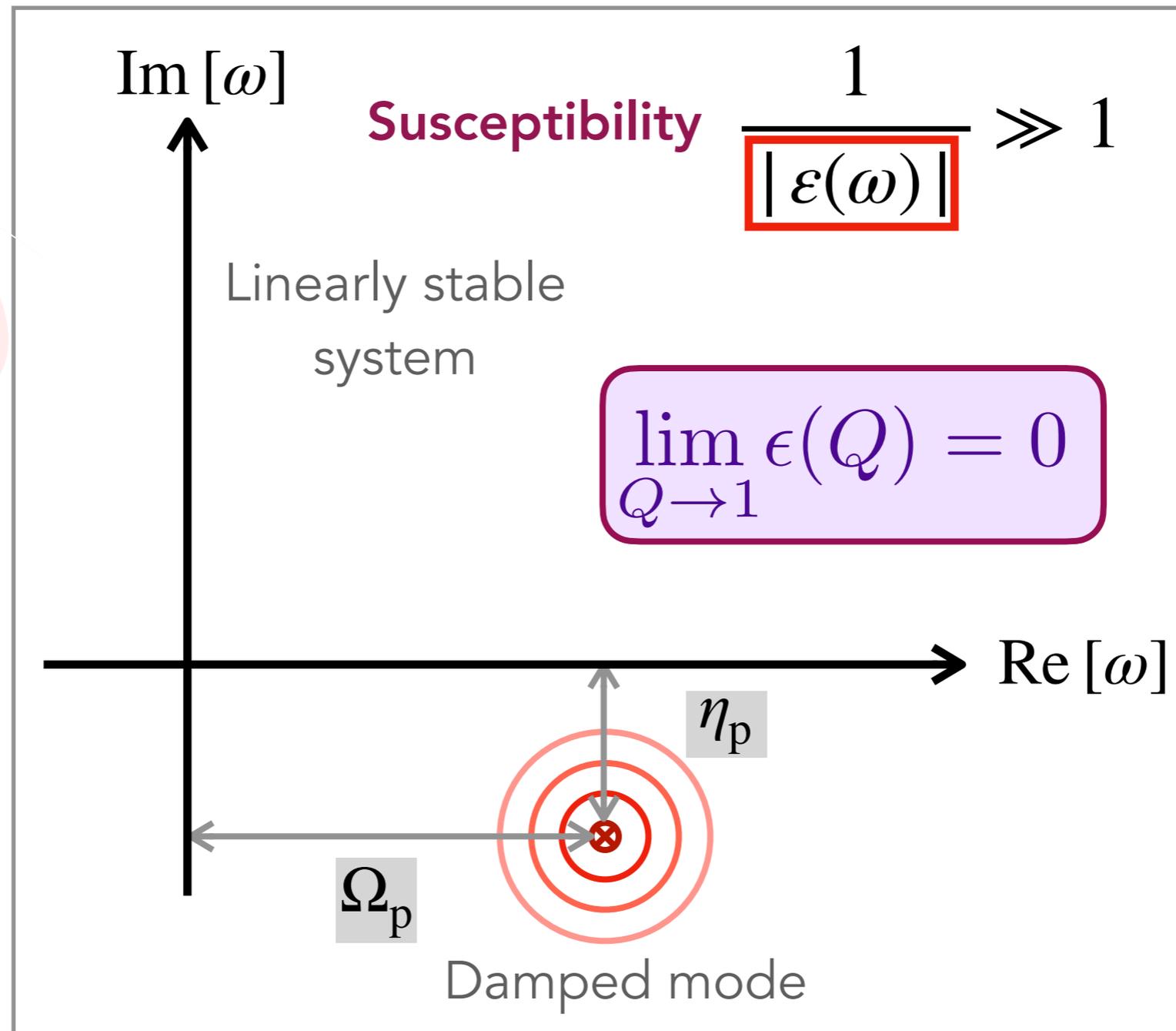
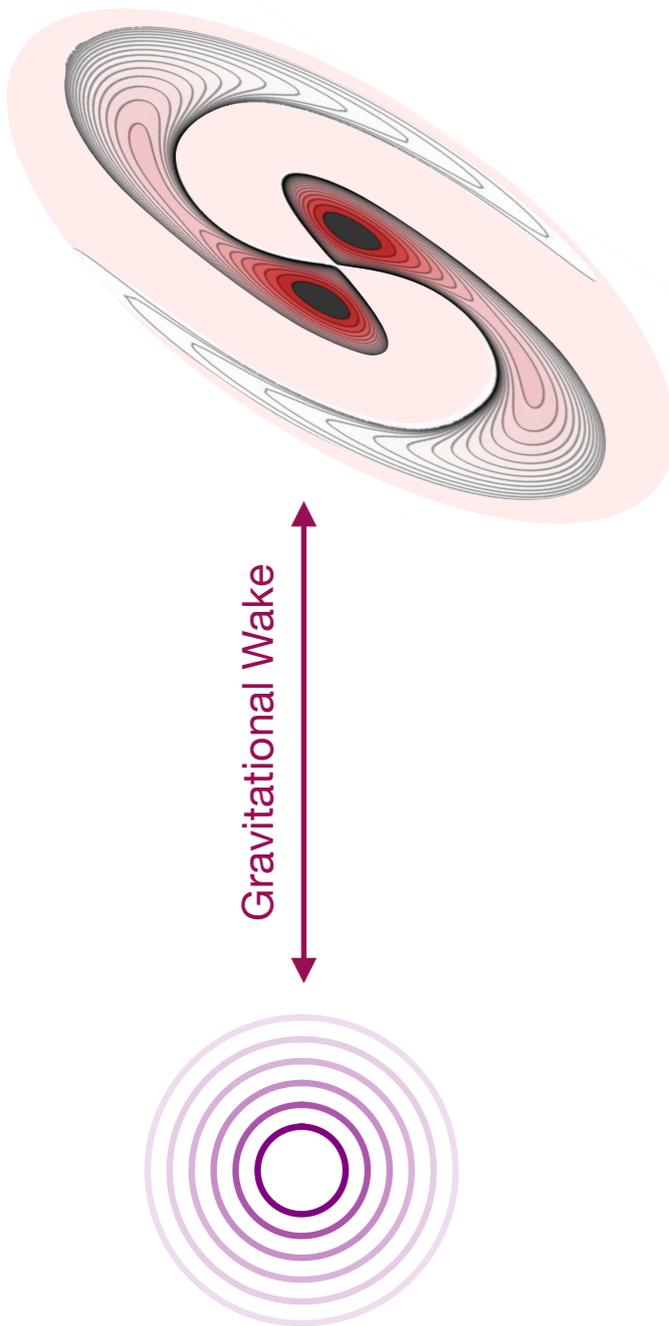
For cold discs...

Gravitational “*Dielectric*” function ϵ

$$\epsilon(Q) \equiv \mathcal{D}(\omega, k) = \det(1 - \mathbf{M}(\omega))$$

Dispersion relation

Response matrix



Wake drastically boost orbital frequencies, stiffening coupling/tightening control loops

Self regulating loop boosted by wake

Transition to secularly-driven morphology promoting self-regulation around an effective Toomre $Q \sim 1$.

Attraction point of feedback loop

$$Q_{\text{eff}}^{-1} = Q_g^{-1} + Q_{\star}^{-1}$$

Destabilising effects

- SN1a
- Turbulence
-
- Minor Mergers
- Misaligned infall
- FlyBys

Star formation and
feedback define
control loop
on disc

Stabilising effects

- Star formation
- Cooling
- Shocks
-
- Co-rotating
Aligned infall

Cosmic
perturbation

Free energy
reservoir
in CGM

$Q \nearrow$

$Q \searrow$

Self regulating loop boosted by wake

Transition to secularly-driven morphology promoting self-regulation around an effective Toomre $Q \sim 1$.

$$T_{\text{dressed}} \simeq |\epsilon| T_{\text{bare}}$$

so long as $T_{\text{dressed}} > T_{\text{cool}}$

Attraction point of feedback loop

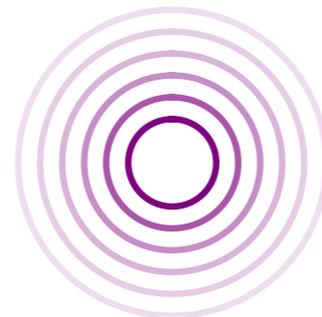
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Destabilising effects

- SN1a
- Turbulence

- Minor Mergers
- Misaligned infall
- FlyBys

Tighter loop



Gravitational Wake

Stabilising effects

- Star formation
- Cooling
- Shocks

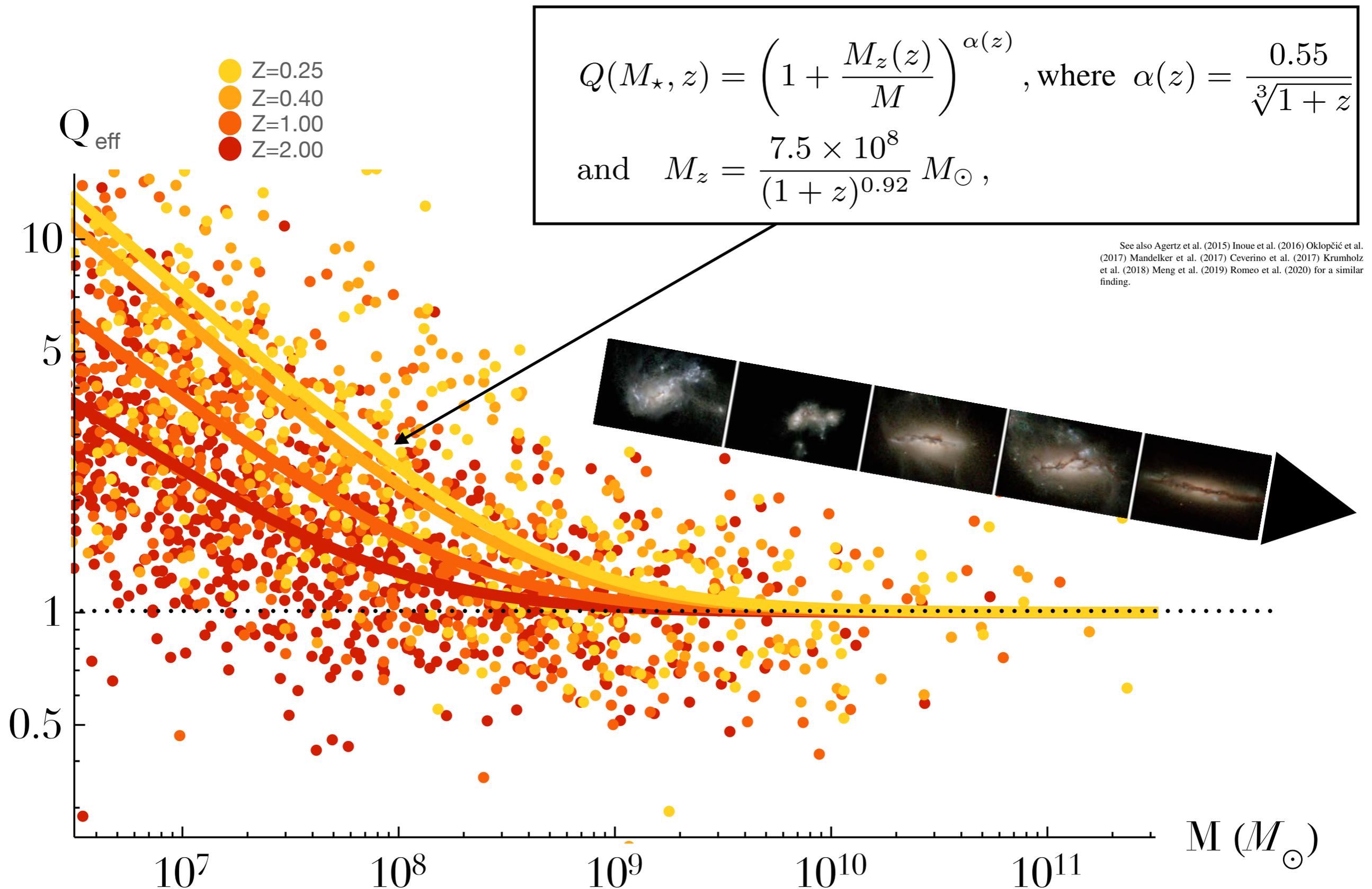
- Co-rotating Aligned infall

Cosmic perturbation

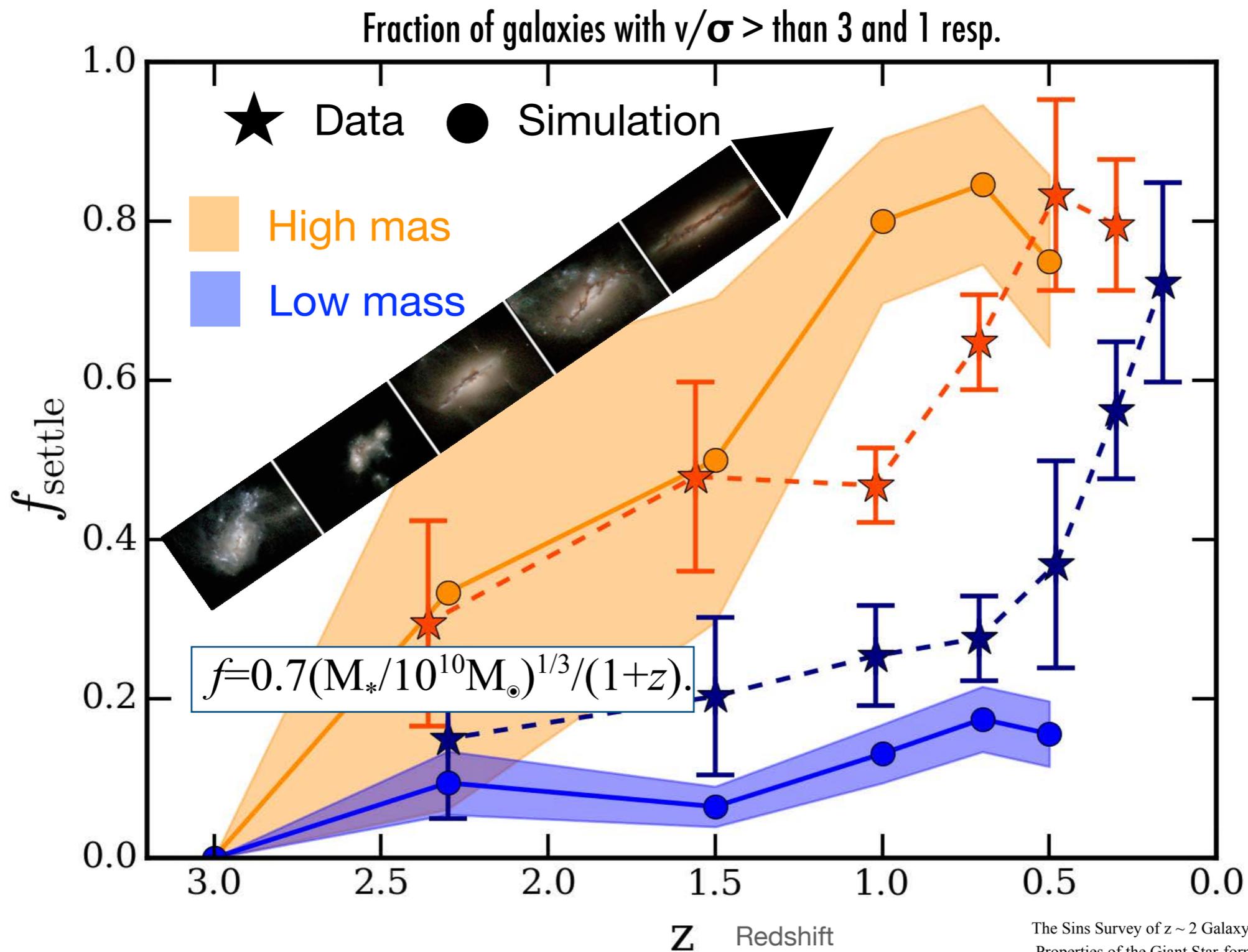
Free energy reservoir in CGM

Open system with control loop generates complexity through self-organisation

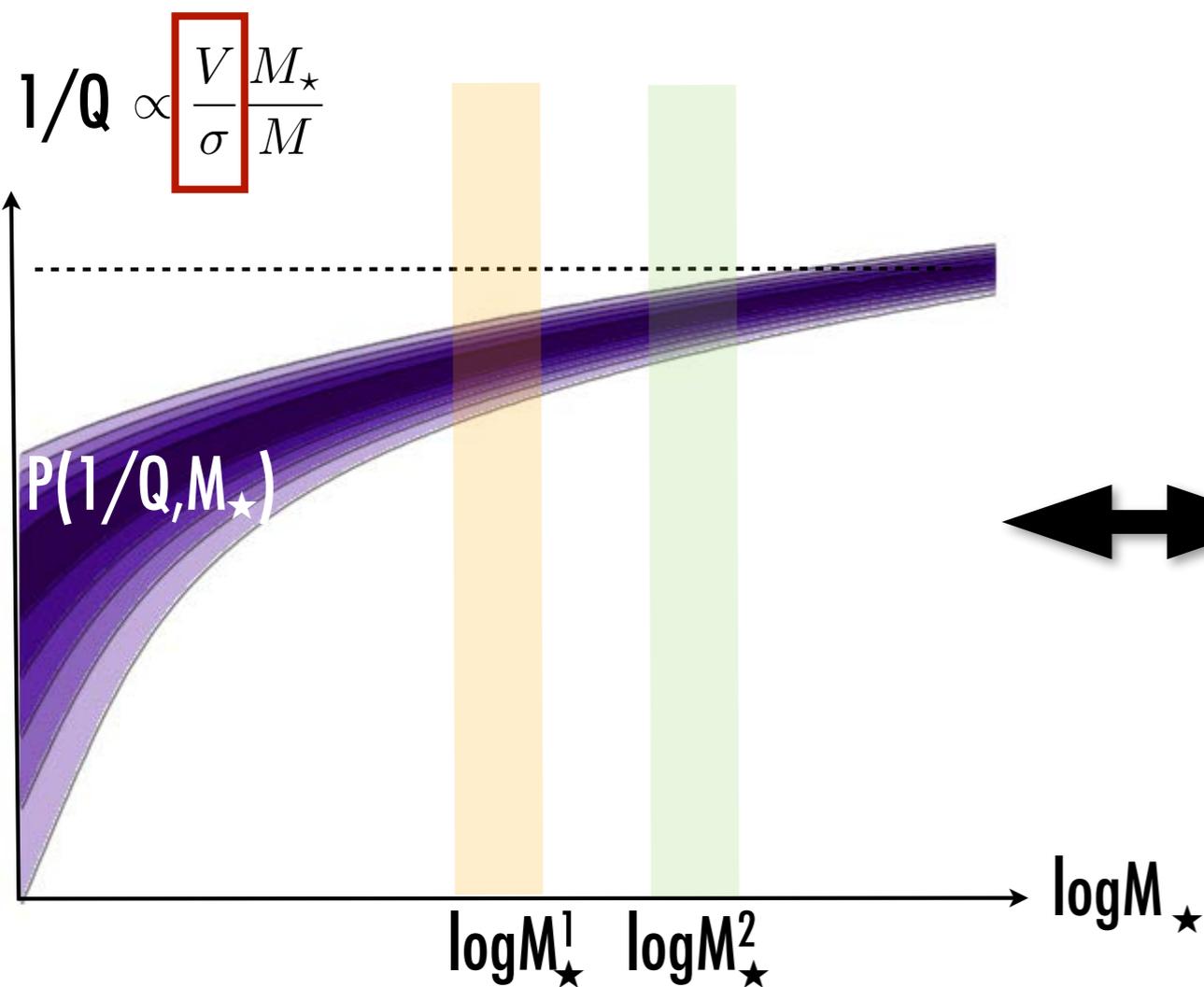
Toomre Q (\star +gas) parameter convergence as a function of *both* mass and redshift



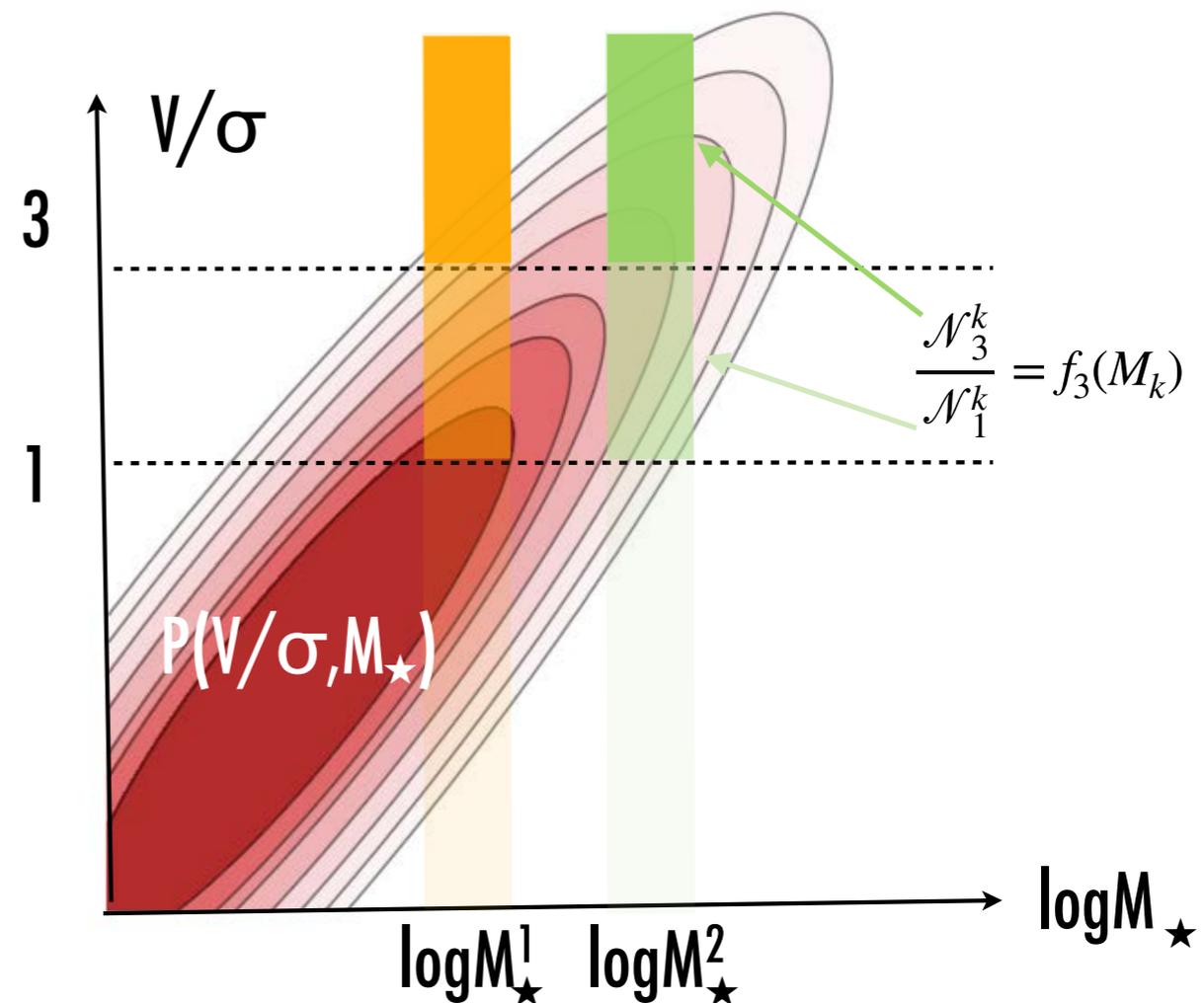
Match between simulation and observation as a function of *both* mass and redshift



Correspondance best expressed while looking at $\text{PDF}(Q, M_\star)$ and $\text{PDF}(V/\sigma, M_\star)$



f_{settle} = Ratio of the integral of the galactic counts over dark (orange or green) regions to that over the light region increases with M_\star



Can this be also explained qualitatively ?

Lagrange Laplace theory of rings (small eccentricity small inclination)

x and y components of angular momentum

$$H(\mathbf{p}, \mathbf{q}) = \frac{1}{2} \mathbf{p}^T \cdot \mathbf{A} \cdot \mathbf{p} + \frac{1}{2} \mathbf{q}^T \cdot \mathbf{A} \cdot \mathbf{q},$$

$$A_{ij} \propto -\frac{G m_i m_j}{\max(R_i, R_j)}$$

In eigenframe of A

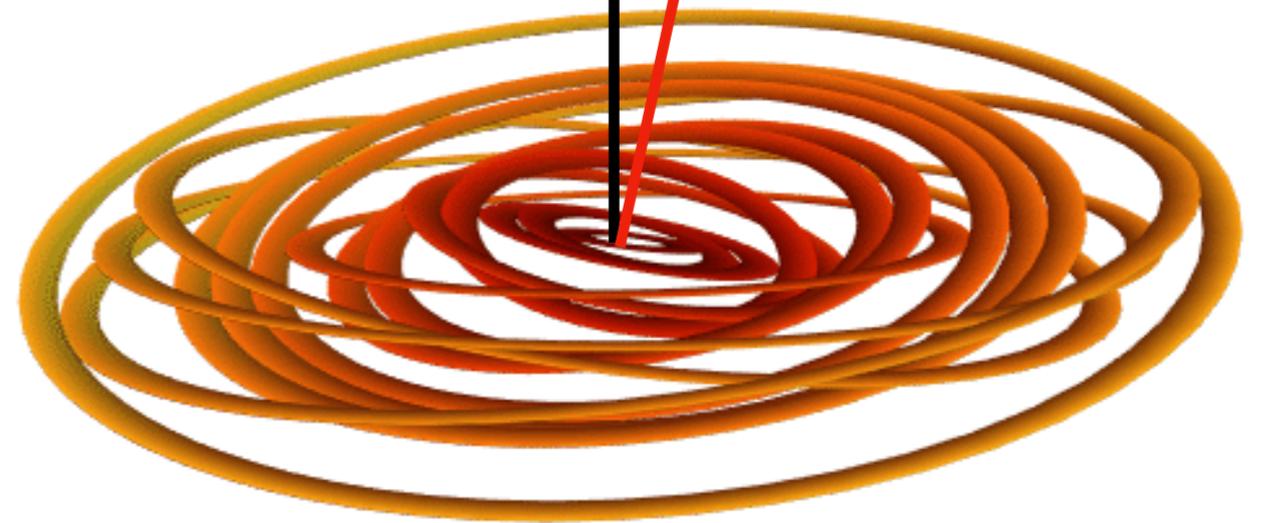
$$\ddot{\hat{q}}_i + \omega_i^2(t) \hat{q}_i = \xi_i$$

Eigen frequency

θ_i, ϕ_i

$$q_i = \gamma_i \theta_i \sin(\phi_i)$$

$$p_i = -\gamma_i \theta_i \cos(\phi_i)$$



Lagrange Laplace theory of rings (small eccentricity small inclination)

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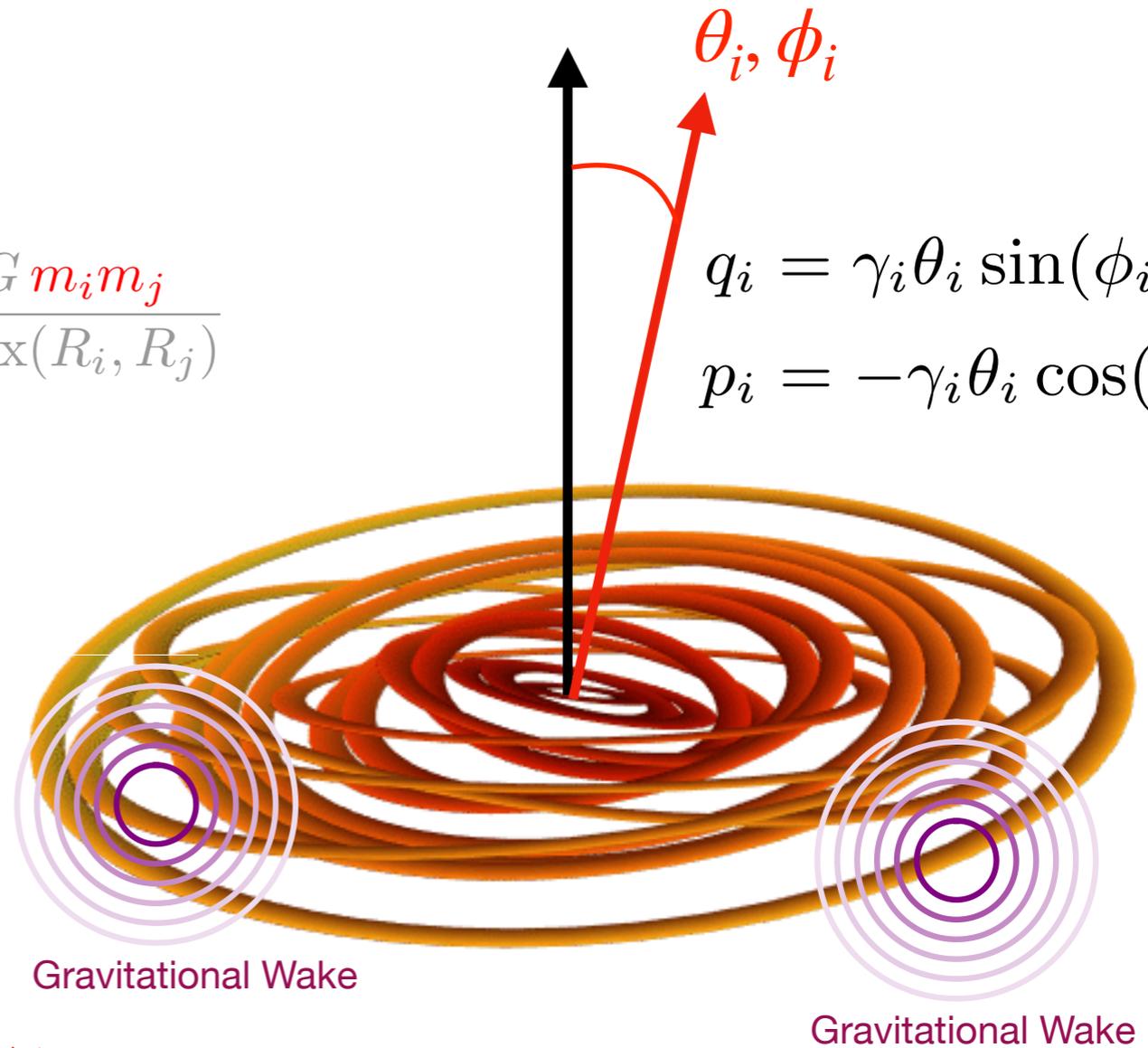
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In eigenframe of A

Eigen frequency

$$\ddot{\hat{q}}_i + \omega_i^2(t) \hat{q}_i = \xi_i$$

$$\omega_i(t) \propto \frac{\omega_{0,i}}{\epsilon(t)}$$

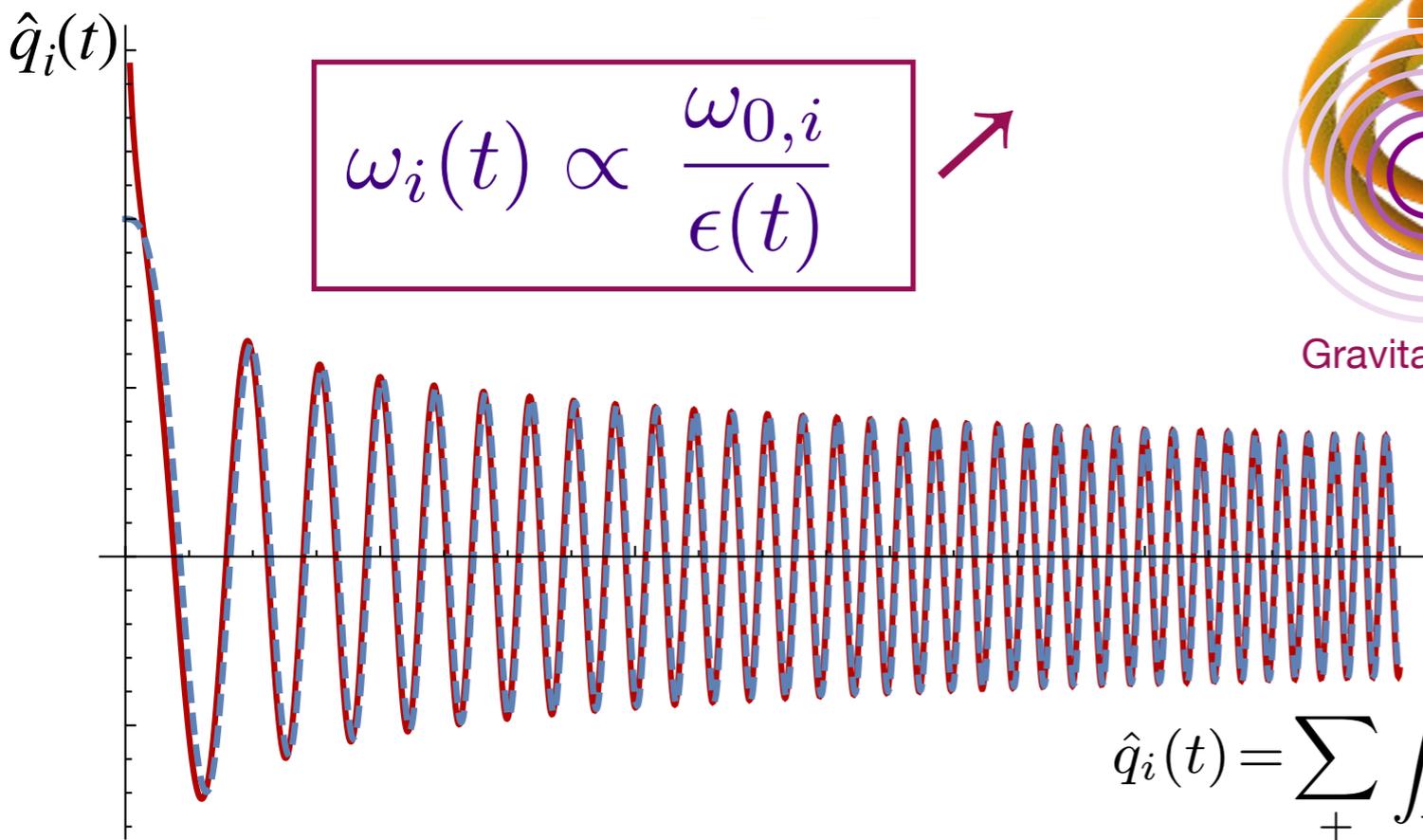


Gravitational Wake

Gravitational Wake

Secular WKB solution

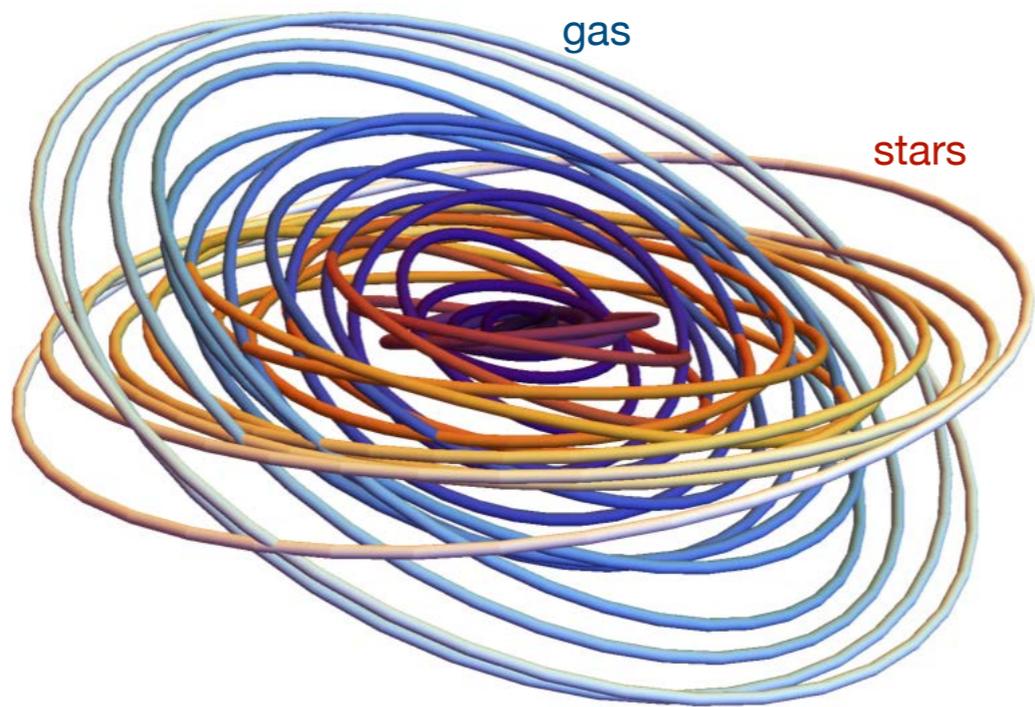
$$\hat{q}_i(t) = \sum_{\pm} \int_{-\infty}^{\infty} \frac{\hat{\xi}_i(t')}{\sqrt{\omega_i(t)\omega_i(t')}} \exp\left(\pm i \int_{t'}^t \omega_i(\tau) d\tau\right) dt'$$



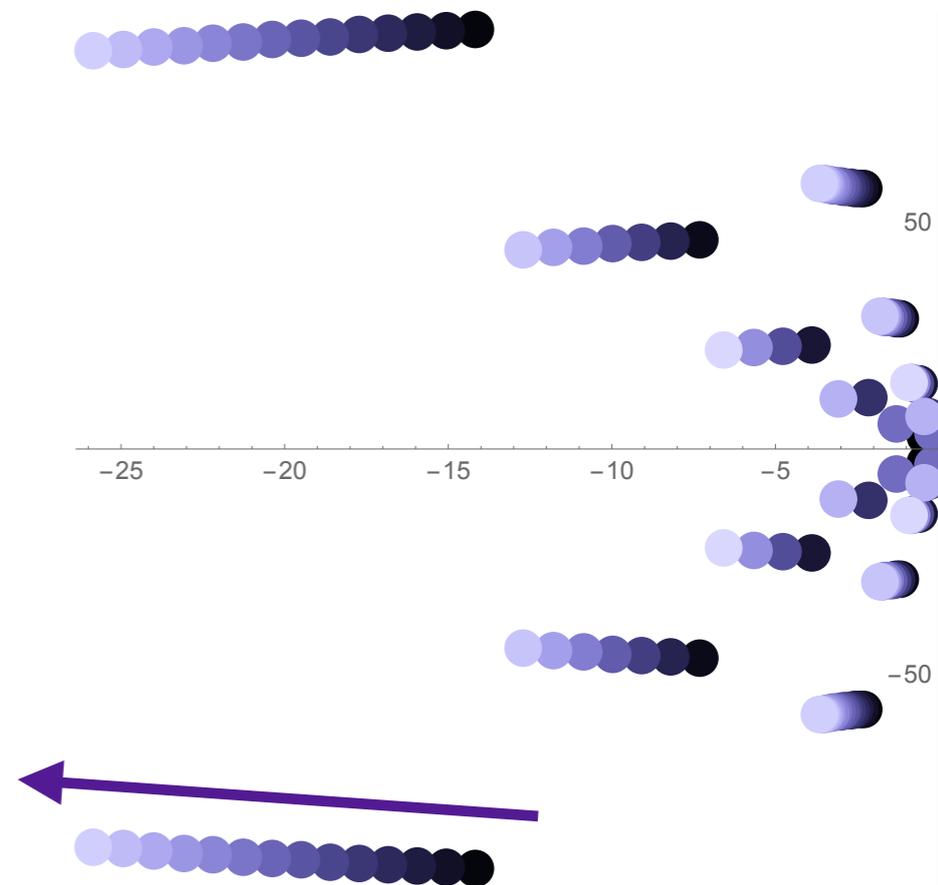
$$\begin{aligned} \ddot{q}_* + \omega_*^2 q_* + \omega_{*g}^2 q_g &= 0, \\ \ddot{q}_g + \omega_g^2 \hat{q}_g + \omega_{*g}^2 q_* + \eta \dot{q}_g &= \xi, \end{aligned}$$

gravitational coupling damping

forcing



Nyquist diagram

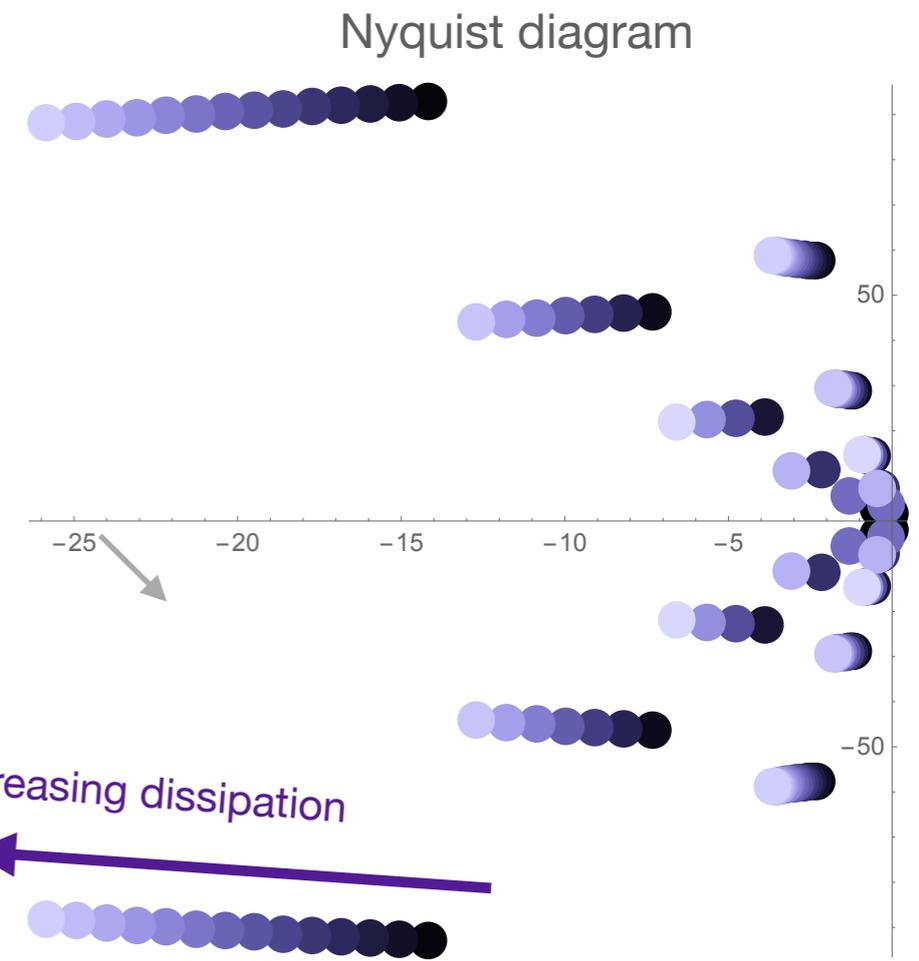
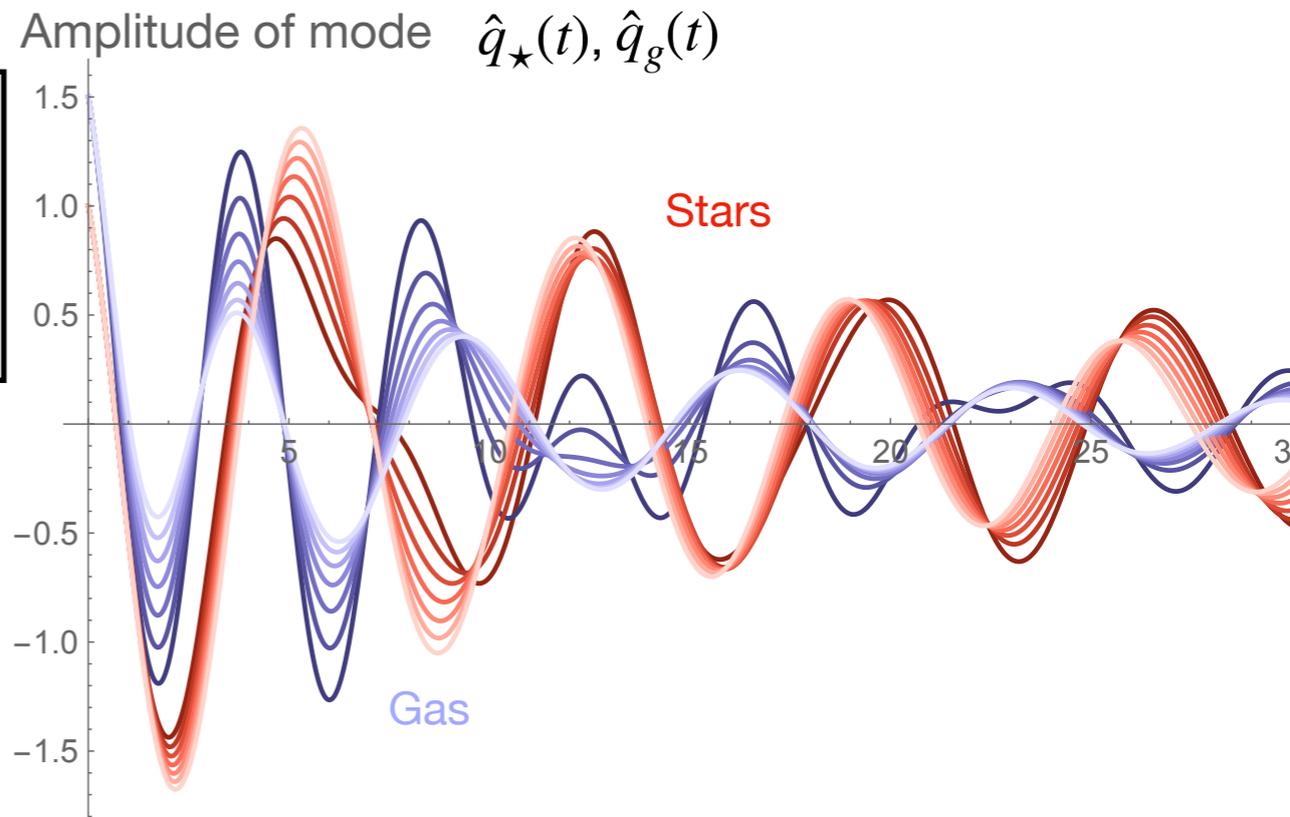
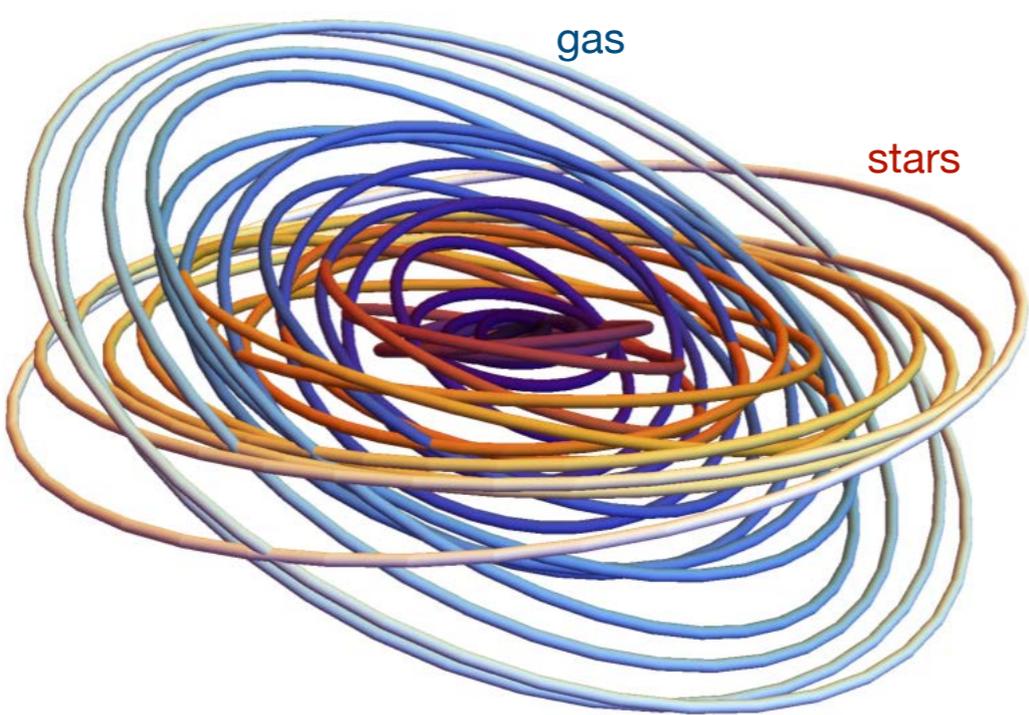


$$q_*(t) = - \sum_{\omega \in S_4} \frac{\omega_{g*}^2 \int_{-\infty}^t \exp((t - \tau)\omega) \xi(\tau) d\tau}{\eta (3\omega^2 + \omega_*^2) + 2\omega (2\omega^2 + \omega_g^2 + \omega_*^2)},$$

$$S_4 = \{\omega \mid (\omega^2 + \omega_*^2) (\omega (\eta + \omega) + \omega_g^2) = \omega_{g*}^4\},$$

Ring gas + star coupling

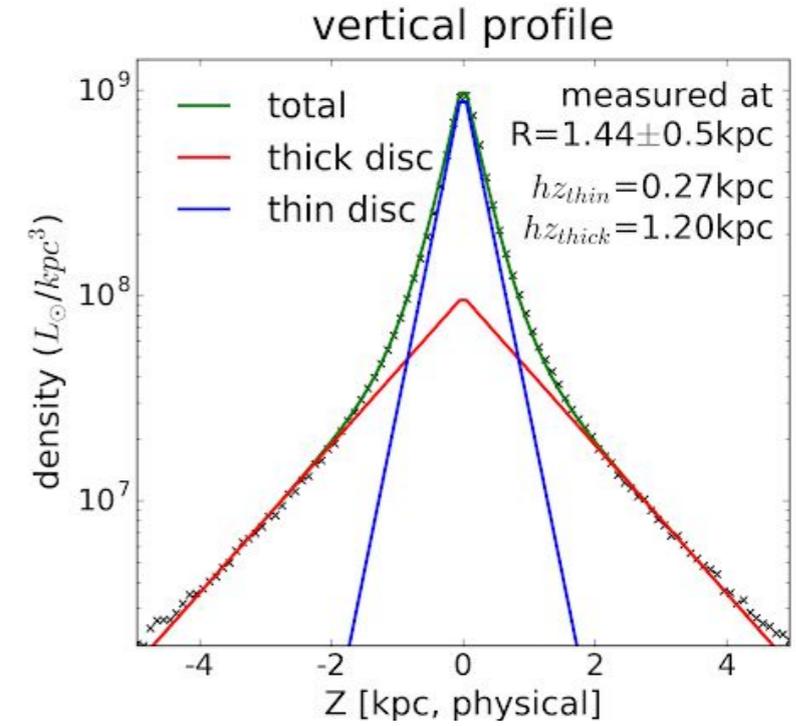
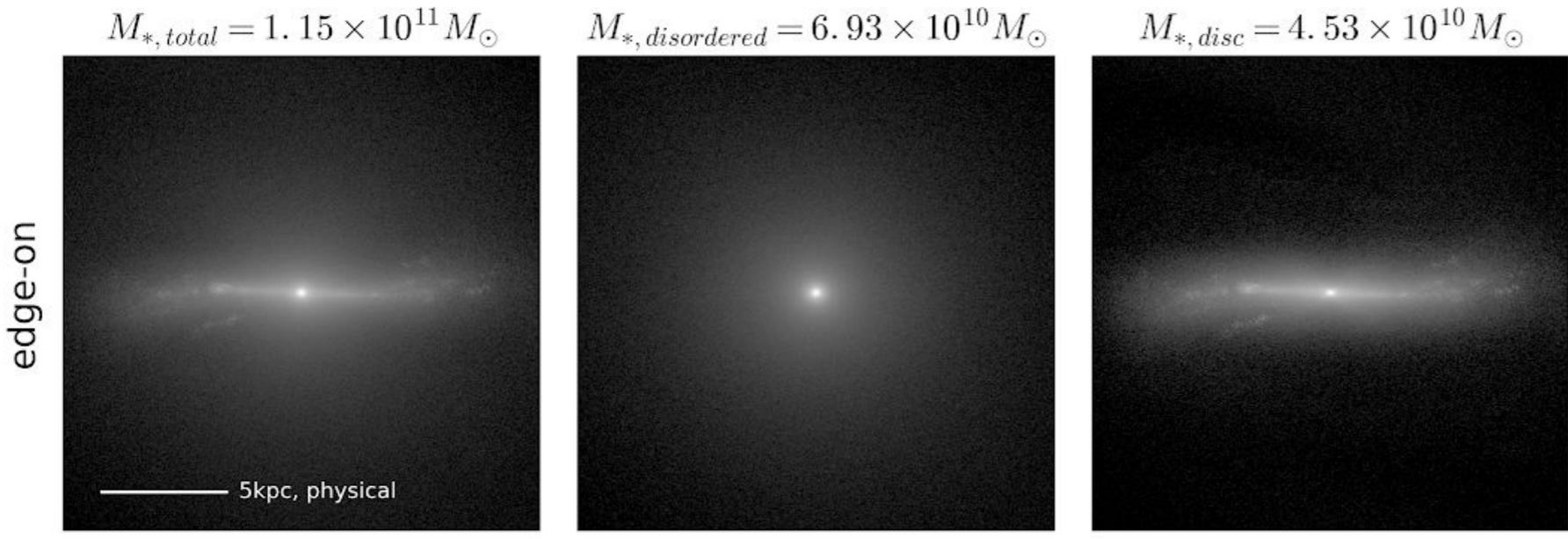
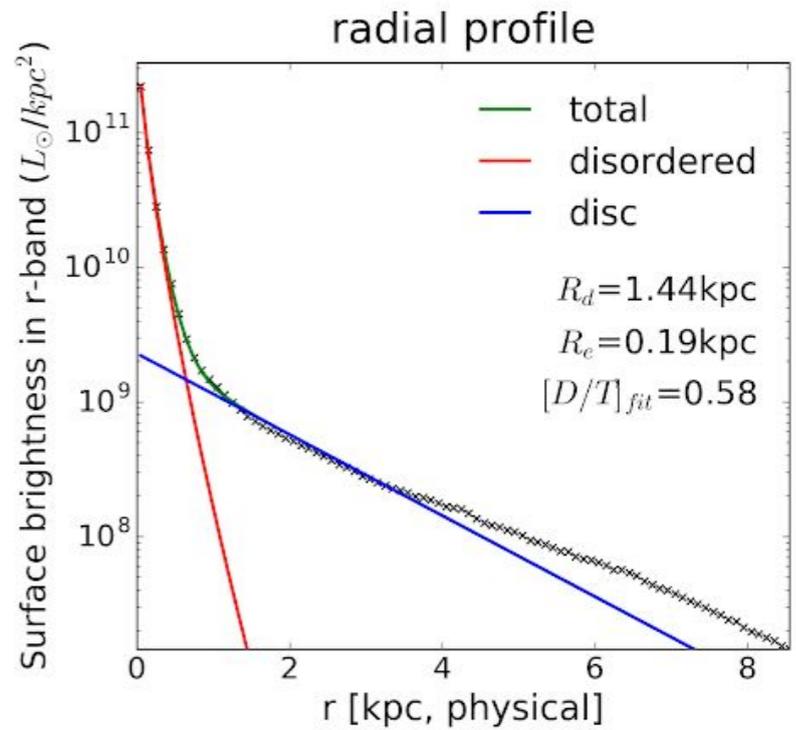
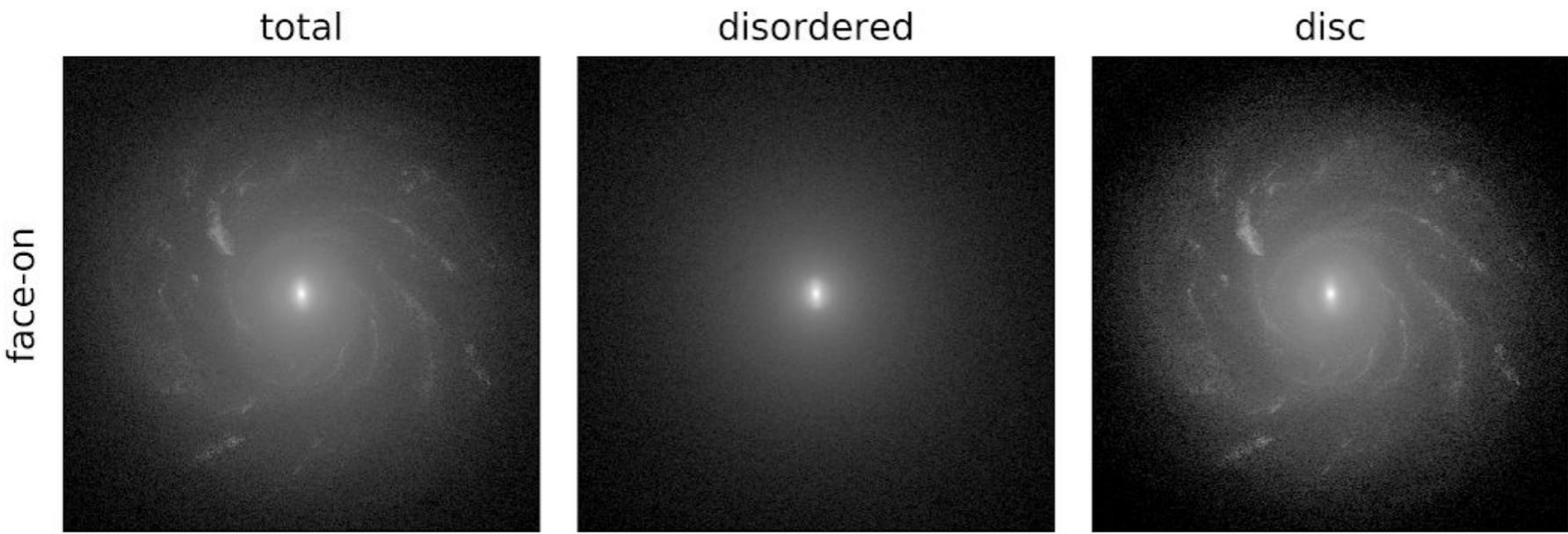
$$\begin{aligned} \ddot{q}_\star + \omega_\star^2 q_\star + \omega_{\star g}^2 q_g &= 0, \\ \ddot{q}_g + \omega_g^2 \hat{q}_g + \omega_{\star g}^2 q_\star + \eta \dot{q}_g &= \xi, \end{aligned}$$



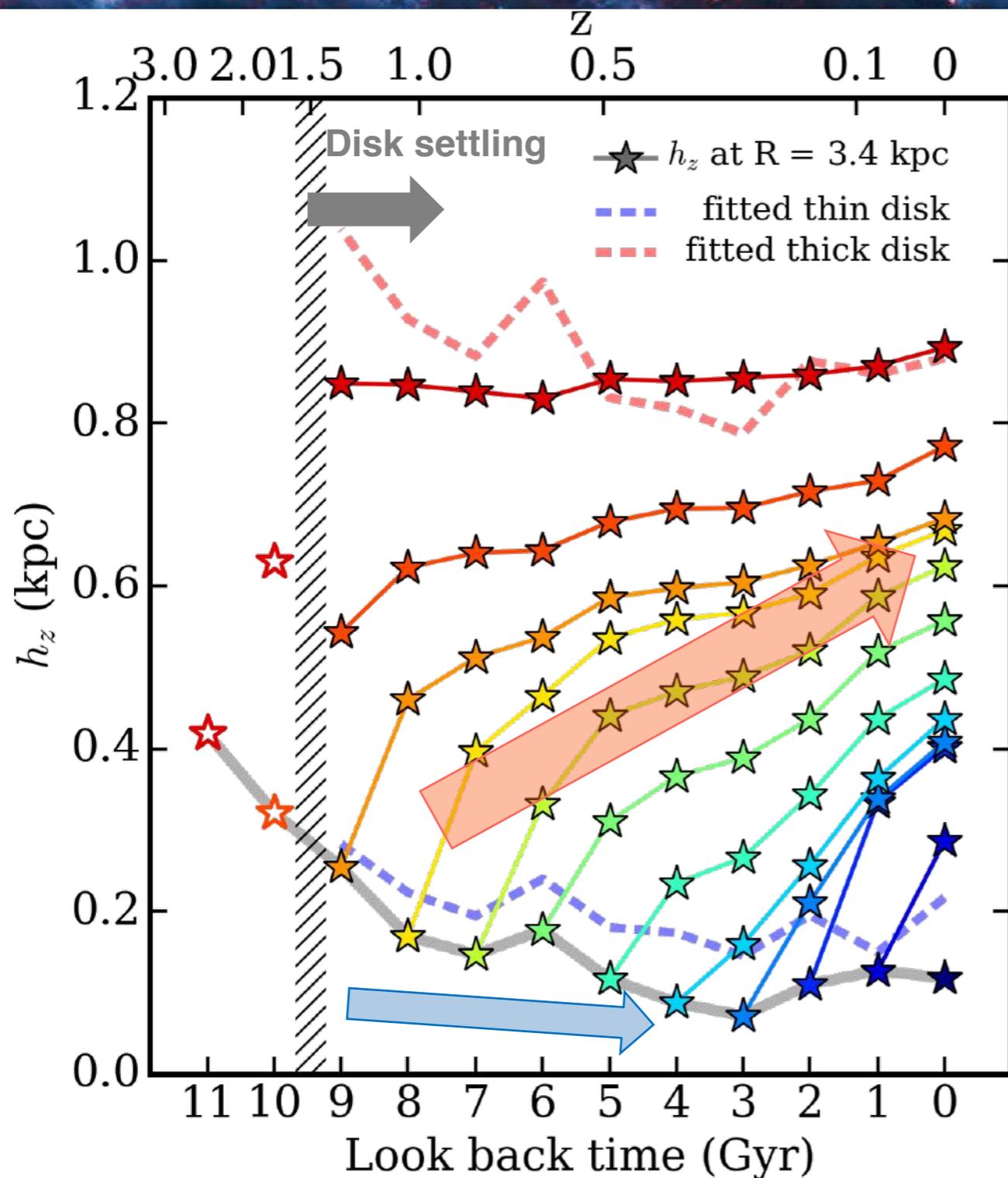
$$q_\star(t) = - \sum_{\omega \in S_4} \frac{\omega_{g\star}^2 \int_{-\infty}^t \exp((t-\tau)\omega) \xi(\tau) d\tau}{\eta(3\omega^2 + \omega_\star^2) + 2\omega(2\omega^2 + \omega_g^2 + \omega_\star^2)},$$

$$S_4 = \{\omega \mid (\omega^2 + \omega_\star^2)(\omega(\eta + \omega) + \omega_g^2) = \omega_{g\star}^4\},$$

*Dissipation in gas **also** brings down the \star modes*



Once in secular mode, the self regulated loop stratifies vertically stars by age, while preserving the total double sech² profile



Pre-existing disk stars get thicker with time due to heating

Galaxy keeps forming in // young thin-disk stars

As a result, the vertical distribution (scale heights of the two components from fit) do not change since disk settling

Vertical orbital diffusion

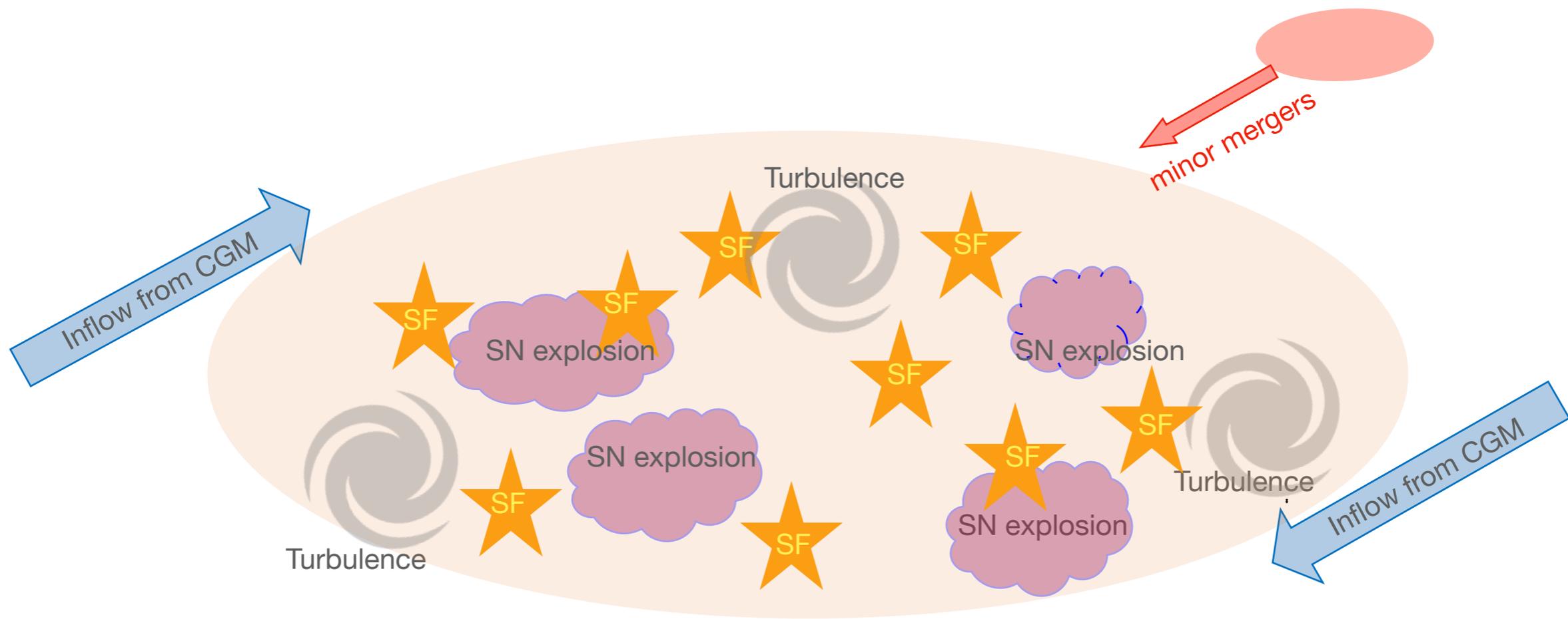
$$D_{\text{diff,dressed}} = \frac{D_{\text{diff,bare}}}{\epsilon(Q)^2}$$

SF efficiency $\frac{\partial \eta_{SF}}{\partial Q} < 0$

Both **star formation** and **vertical orbital diffusion** are regulated by same ($Q \rightarrow 1$) **confounding** factor which produce stars and diffuse the stellar orbital structure.

The stellar thick disc is simply the **secular remnant** of the disc settling process.

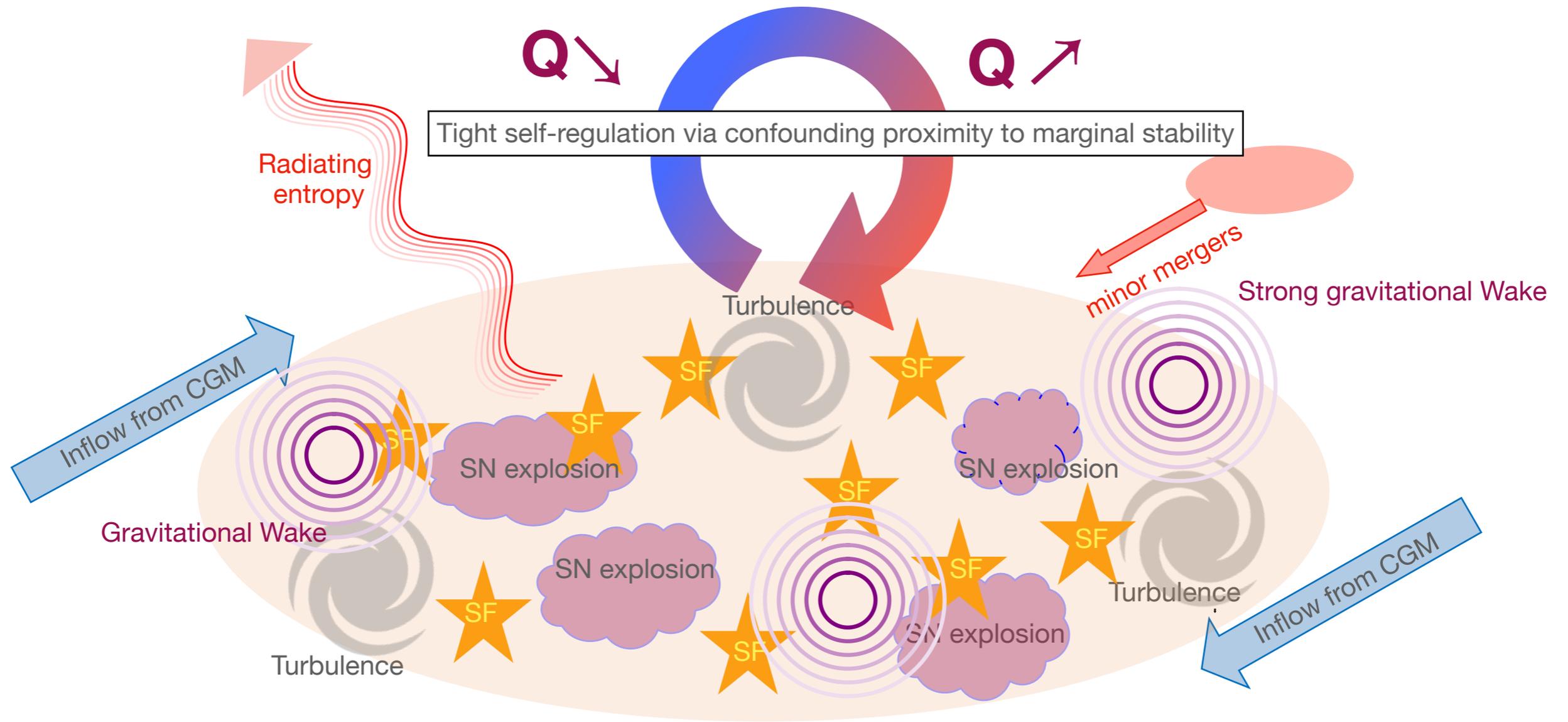
Conclusion: wakes redefines clocks



From a complex picture...

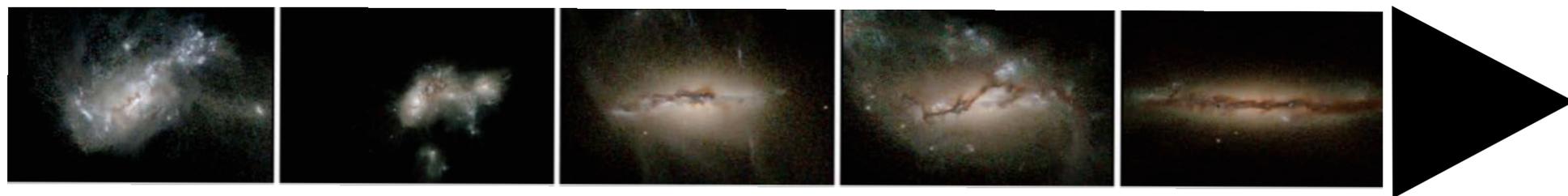


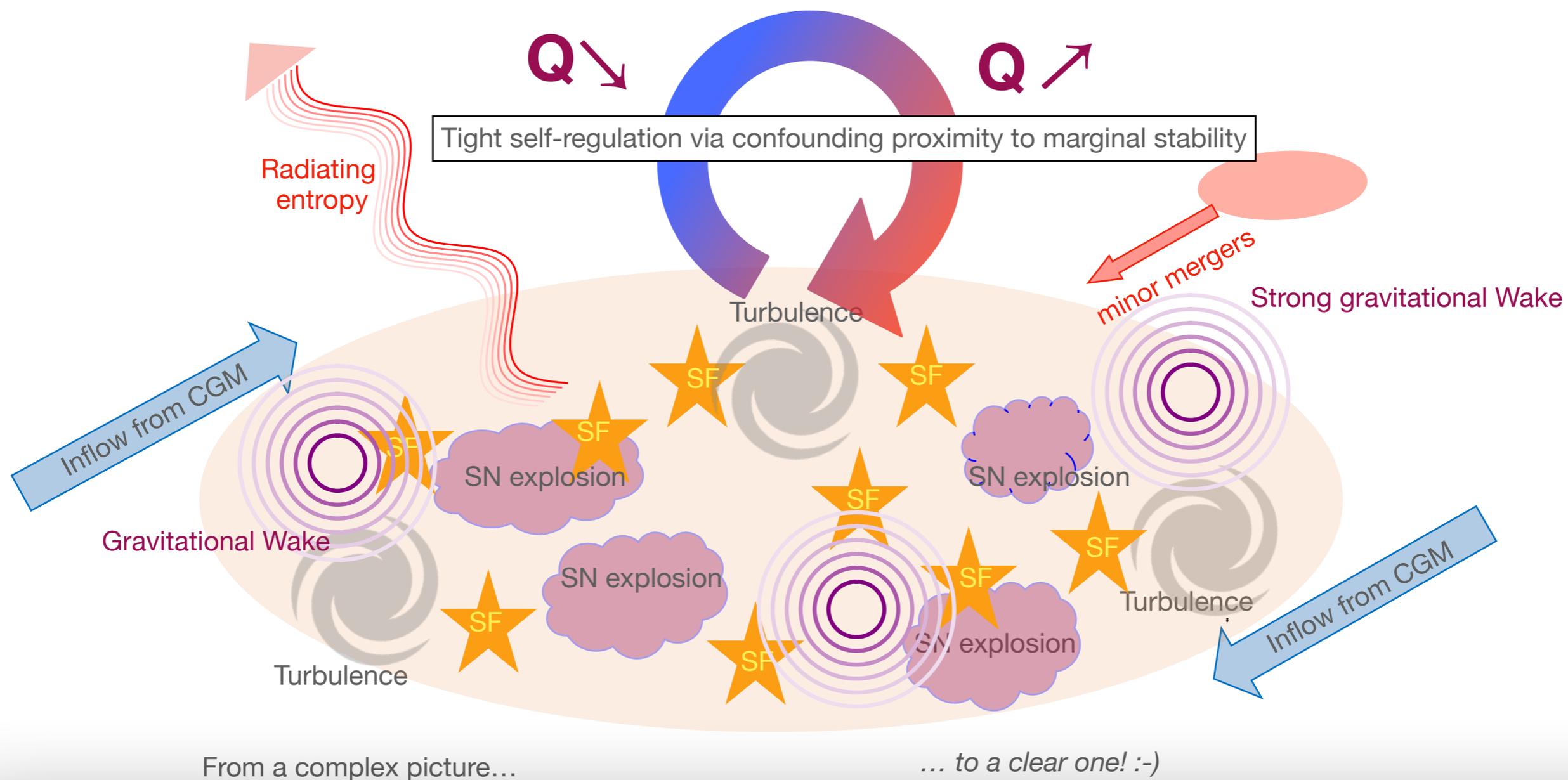
Conclusion: wakes redefines clocks



From a complex picture...

... to a clear one! :-)





Thin galactic disks are **emerging** structures of hierarchical clustering when secular processes take over.

Appearance of improbable structure is **paradoxically** made possible by shocks, feedback and turbulence in disc.

Processes radiates entropy, and **wakes** tightens a **self-regulating** loop towards **marginal stability**, pumping free (rotational) energy from the CGM. **Wake** also tightens re-alignment.

Link to maximum entropy production??

Proximity to marginal stability acts as **confounding** factor for thickening and star formation, explaining stratification of thin and **thick** disc (Yi's talk).